

1. Simplify

$$\frac{7 + \sqrt{5}}{\sqrt{5} - 1}$$

giving your answer in the form $a + b\sqrt{5}$, where a and b are integers.

(4)

Q1

(Total 4 marks)



4. A sequence a_1, a_2, a_3, \dots is defined by

$$a_1 = 4$$
$$a_{n+1} = k(a_n + 2), \quad \text{for } n \geq 1$$

where k is a constant.

- (a) Find an expression for a_2 in terms of k .

(1)

Given that $\sum_{i=1}^3 a_i = 2$,

- (b) find the two possible values of k .

(6)



5. Find the set of values of x for which

(a) $2(3x + 4) > 1 - x$ **(2)**

(b) $3x^2 + 8x - 3 < 0$ **(4)**



8.

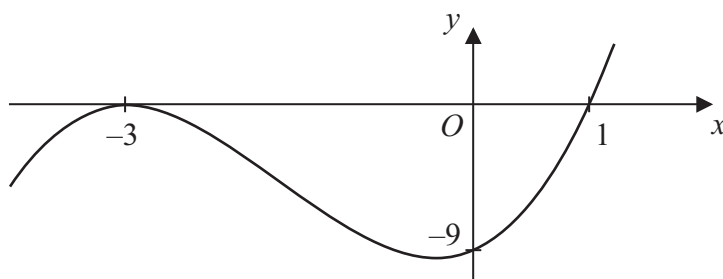


Figure 1

Figure 1 shows a sketch of the curve with equation $y = f(x)$ where

$$f(x) = (x + 3)^2 (x - 1), \quad x \in \mathbb{R}.$$

The curve crosses the x -axis at $(1, 0)$, touches it at $(-3, 0)$ and crosses the y -axis at $(0, -9)$

- (a) In the space below, sketch the curve C with equation $y = f(x + 2)$ and state the coordinates of the points where the curve C meets the x -axis. **(3)**
- (b) Write down an equation of the curve C . **(1)**
- (c) Use your answer to part (b) to find the coordinates of the point where the curve C meets the y -axis. **(2)**



Question 8 continued

Q8

(Total 6 marks)



P 4 1 8 0 2 A 0 1 7 2 8

9.

$$f'(x) = \frac{(3 - x^2)^2}{x^2}, \quad x \neq 0$$

(a) Show that $f'(x) = 9x^{-2} + A + Bx^2$,

where A and B are constants to be found. (3)

(b) Find $f''(x)$. (2)

Given that the point $(-3, 10)$ lies on the curve with equation $y = f(x)$,

(c) find $f(x)$. (5)



10. Given the simultaneous equations

$$\begin{aligned} 2x + y &= 1 \\ x^2 - 4ky + 5k &= 0 \end{aligned}$$

where k is a non zero constant,

(a) show that

$$x^2 + 8kx + k = 0 \tag{2}$$

Given that $x^2 + 8kx + k = 0$ has equal roots,

(b) find the value of k . (3)

(c) For this value of k , find the solution of the simultaneous equations. (3)



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Question 10 continued

Lined area for writing the answer to Question 10.

(Total 8 marks)

Q10



P 4 1 8 0 2 A 0 2 3 2 8

11.

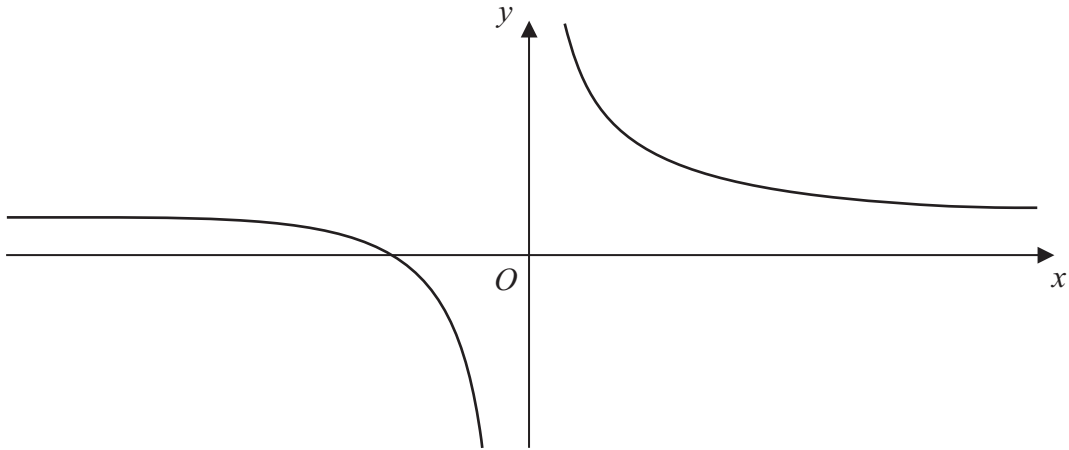


Figure 2

Figure 2 shows a sketch of the curve H with equation $y = \frac{3}{x} + 4$, $x \neq 0$.

(a) Give the coordinates of the point where H crosses the x -axis. (1)

(b) Give the equations of the asymptotes to H . (2)

(c) Find an equation for the normal to H at the point $P(-3, 3)$. (5)

This normal crosses the x -axis at A and the y -axis at B .

(d) Find the length of the line segment AB . Give your answer as a surd. (3)



