

# Coordinate Geometry

## Question Paper

Level	Pre U
Subject	Maths
Exam Board	Cambridge International Examinations
Topic	Coordinate Geometry
Booklet	Question Paper

**Time Allowed:** 88 minutes

**Score:** /73

**Percentage:** /100

**Grade Boundaries:**

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1 A circle has equation  $(x - 4)^2 + (y + 7)^2 = 64$ .

(i) Write down the coordinates of the centre and the radius of the circle. [2]

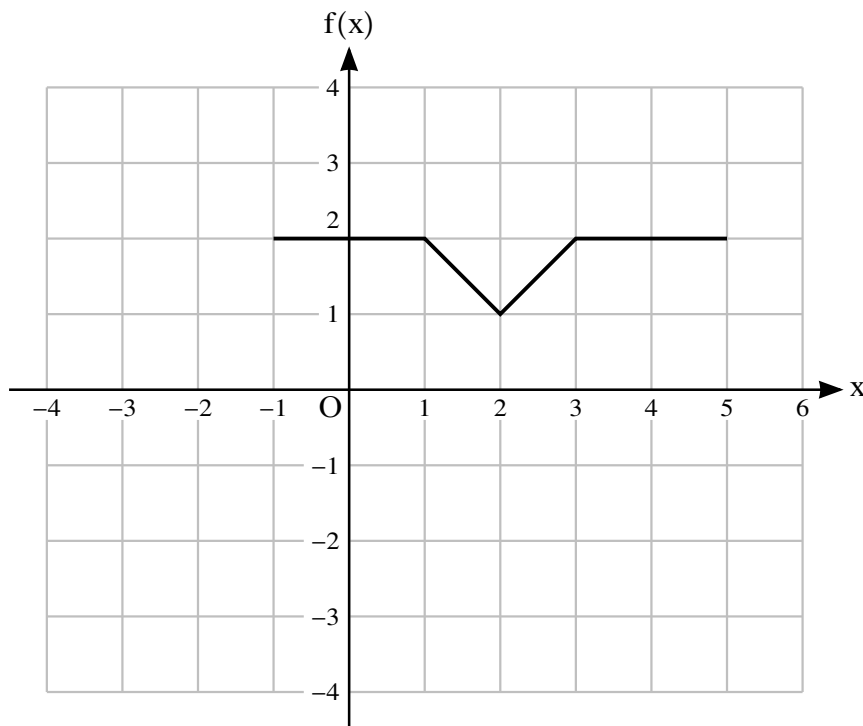
Two points,  $A$  and  $B$ , lie on the circle and have coordinates  $(4, 1)$  and  $(12, -7)$  respectively.

(ii) Find the coordinates of the midpoint of the chord  $AB$ . [2]

2 (i) The points  $A$  and  $B$  have coordinates  $(-4, 4)$  and  $(8, 1)$  respectively. Find the equation of the line  $AB$ .  
Give your answer in the form  $y = mx + c$ . [3]

(ii) Determine, with a reason, whether the line  $y = 7 - 4x$  is perpendicular to the line  $AB$ . [2]

3 The graph of  $f(x)$  is shown below.



Draw the graphs of

(i)  $f(x + 2) + 1$ , [2]

(ii)  $-\frac{1}{2}f(x)$ . [2]

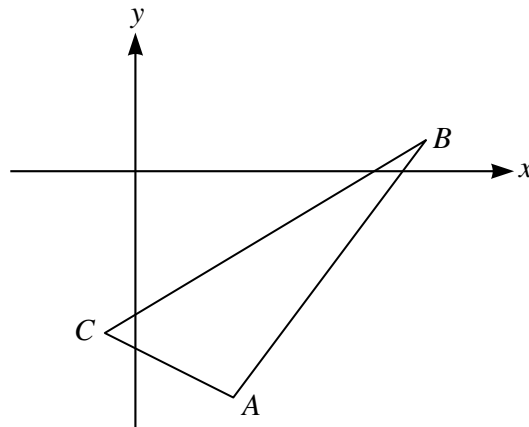
4 The points A, B, C and D have coordinates (2, -1, 0), (3, 2, 5), (4, 2, 3) and (-1, a, b) respectively, where a and b are constants.

(i) Find the angle ABC. [4]

(ii) Given that the lines AB and CD are parallel, find the values of a and b. [3]

5 A is the point (2, 1) and B is the point (10, 7). Find the coordinates of the mid-point of AB and the length of AB [3]

6



The diagram shows a triangle ABC. The vertices have coordinates A (3, -7), B (9, 1) and C (-1, -5).

(i) (a) Find the length of the side AB. [2]

(b) Find the coordinates of the mid-point of AB. [1]

(c) A circle has diameter AB. Find the equation of the circle in the form  $(x - a)^2 + (y - b)^2 = r^2$ , where a, b and r are constants to be found. [3]

(ii) Find the equation of the line l passing through B parallel to AC. [3]

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- 7 Find the equation of the line passing through the points  $(-2, 5)$  and  $(4, -7)$ . Give your answer in the form  $y = mx + c$ . [3]

- 8 Functions  $f$ ,  $g$  and  $h$  are defined for  $x \in \mathbb{R}$  by

$$f : x \mapsto x^2 - 2x,$$

$$g : x \mapsto x^2,$$

$$h : x \mapsto \sin x.$$

- (i) (a) State whether or not  $f$  has an inverse, giving a reason. [2]  
(b) Determine the range of the function  $f$ . [2]
- (ii) (a) Show that  $gh(x)$  can be expressed as  $\frac{1}{2}(1 - \cos 2x)$ . [2]  
(b) Sketch the curve  $C$  defined by  $y = gh(x)$  for  $0 \leq x \leq 2\pi$ . [3]

- 9 The curve  $y = x^2$  intersects the line  $y = kx$ ,  $k > 0$ , at the origin and the point  $P$ . The region bounded by the curve and the line, between the origin and  $P$ , is denoted by  $R$ .

- (i) Show that the area of the region  $R$  is  $\frac{1}{6}k^3$ . [3]

The line  $x = a$  cuts the region  $R$  into two parts of equal area.

- (ii) Show that  $k^3 - 6a^2k + 4a^3 = 0$ . [3]

The gradient of the line  $y = kx$  increases at a constant rate with respect to time  $t$ . Given that  $\frac{dk}{dt} = 2$ ,

- (iii) determine the value of  $\frac{da}{dt}$  when  $a = 1$  and  $k = 2$ , [4]

- (iv) determine the value of  $\frac{da}{dt}$  when  $a = 1$  and  $k \neq 2$ , expressing your answer in the form  $p + q\sqrt{3}$ , where  $p$  and  $q$  are integers. [5]

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- 10 The point  $F$  has coordinates  $(0, a)$  and the straight line  $D$  has equation  $y = b$ , where  $a$  and  $b$  are constants with  $a > b$ . The curve  $C$  consists of points equidistant from  $F$  and  $D$ .

- (i) Show that the cartesian equation of  $C$  can be expressed in the form

$$y = \frac{1}{2(a-b)}x^2 + \frac{1}{2}(a+b). \quad [3]$$

- (ii) State the  $y$ -coordinate of the lowest point of the curve and prove that  $F$  and  $D$  are on opposite sides of  $C$ . [2]

- (iii) (a) The point  $P$  on the curve has  $x$ -coordinate  $\sqrt{a^2 - b^2}$ , where  $|a| > |b|$ . Show that the tangent at  $P$  passes through the origin. [4]

- (b) The tangent at  $P$  intersects the line  $D$  at the point  $Q$ . In the case that  $a = 12$  and  $b = -8$ , find the coordinates of  $P$  and  $Q$ . Show that the length of  $PQ$  can be expressed as  $p\sqrt{q}$ , where  $p = 2q$ . [5]