

Write your name here

Surname

Other names

**Pearson Edexcel**  
**Level 3 GCE**

Centre Number

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Candidate Number

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# Further Mathematics

**Advanced**

**Paper 1: Core Pure Mathematics 1**

Sample Assessment Material for first teaching September 2017

**Time: 1 hour 30 minutes**

Paper Reference

**9FM0/01**

**You must have:**

Mathematical Formulae and Statistical Tables, calculator

Total Marks

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**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

## Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Answer ALL questions. Write your answers in the spaces provided.

1. Prove that

$$\sum_{r=1}^n \frac{1}{(r+1)(r+3)} = \frac{n(an+b)}{12(n+2)(n+3)}$$

where  $a$  and  $b$  are constants to be found.

(5)

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2. Prove by induction that for all positive integers  $n$ ,

$$f(n) = 2^{3n+1} + 3(5^{2n+1})$$

is divisible by 17

(6)

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3.

$$f(z) = z^4 + az^3 + 6z^2 + bz + 65$$

where  $a$  and  $b$  are real constants.

Given that  $z = 3 + 2i$  is a root of the equation  $f(z) = 0$ , show the roots of  $f(z) = 0$  on a single Argand diagram.

(9)

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4.

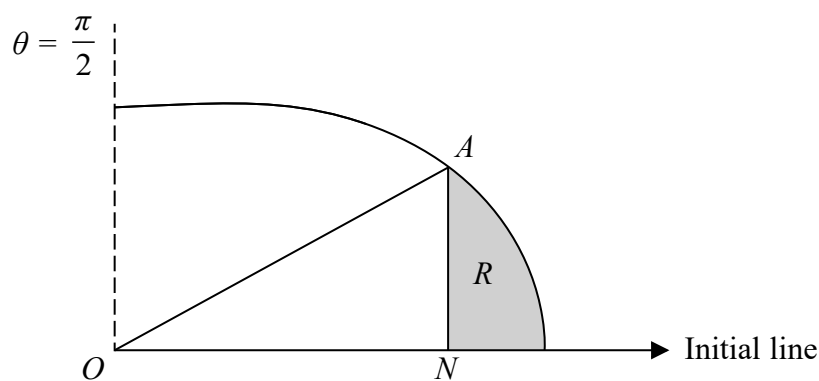


Figure 1

The curve  $C$  shown in Figure 1 has polar equation

$$r = 4 + \cos 2\theta \quad 0 \leq \theta \leq \frac{\pi}{2}$$

At the point  $A$  on  $C$ , the value of  $r$  is  $\frac{9}{2}$

The point  $N$  lies on the initial line and  $AN$  is perpendicular to the initial line.

The finite region  $R$ , shown shaded in Figure 1, is bounded by the curve  $C$ , the initial line and the line  $AN$ .

Find the exact area of the shaded region  $R$ , giving your answer in the form  $p\pi + q\sqrt{3}$  where  $p$  and  $q$  are rational numbers to be found.

(9)





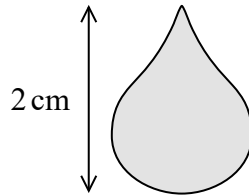








7.



**Figure 2**

Figure 2 shows the image of a gold pendant which has height 2 cm. The pendant is modelled by a solid of revolution of a curve  $C$  about the  $y$ -axis. The curve  $C$  has parametric equations

$$x = \cos \theta + \frac{1}{2} \sin 2\theta, \quad y = -(1 + \sin \theta) \quad 0 \leq \theta \leq 2\pi$$

(a) Show that a Cartesian equation of the curve  $C$  is

$$x^2 = -(y^4 + 2y^3) \tag{4}$$

(b) Hence, using the model, find, in  $\text{cm}^3$ , the volume of the pendant.

(4)

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8. The line  $l_1$  has equation  $\frac{x-2}{4} = \frac{y-4}{-2} = \frac{z+6}{1}$

The plane  $\Pi$  has equation  $x - 2y + z = 6$

The line  $l_2$  is the reflection of the line  $l_1$  in the plane  $\Pi$ .

Find a vector equation of the line  $l_2$

(7)

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