

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel  
Level 3 GCE**

Centre Number

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Candidate Number

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**Monday 3 June 2019**

Morning (Time: 1 hour 30 minutes)

Paper Reference **9FM0/01**

**Further Mathematics**

**Advanced**

**Paper 1: Core Pure Mathematics 1**

**You must have:**

Mathematical Formulae and Statistical Tables (Green), calculator

Total Marks

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**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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**Question 1 continued**

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**Question 1 continued**

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**(Total for Question 1 is 9 marks)**



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2. Show that

$$\int_0^{\infty} \frac{8x - 12}{(2x^2 + 3)(x + 1)} dx = \ln k$$

where  $k$  is a rational number to be found.

(7)

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Question 2 continued

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4. Prove that, for  $n \in \mathbb{Z}, n \geq 0$

$$\sum_{r=0}^n \frac{1}{(r+1)(r+2)(r+3)} = \frac{(n+a)(n+b)}{c(n+2)(n+3)}$$

where  $a, b$  and  $c$  are integers to be found.

(5)

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7. The line  $l_1$  has equation

$$\frac{x-1}{2} = \frac{y+1}{-1} = \frac{z-4}{3}$$

The line  $l_2$  has equation

$$\mathbf{r} = \mathbf{i} + 3\mathbf{k} + t(\mathbf{i} - \mathbf{j} + 2\mathbf{k})$$

where  $t$  is a scalar parameter.

- (a) Show that  $l_1$  and  $l_2$  lie in the same plane. (3)
- (b) Write down a vector equation for the plane containing  $l_1$  and  $l_2$ . (1)
- (c) Find, to the nearest degree, the acute angle between  $l_1$  and  $l_2$ . (3)











8. A scientist is studying the effect of introducing a population of white-clawed crayfish into a population of signal crayfish.

At time  $t$  years, the number of white-clawed crayfish,  $w$ , and the number of signal crayfish,  $s$ , are modelled by the differential equations

$$\frac{dw}{dt} = \frac{5}{2}(w - s)$$
$$\frac{ds}{dt} = \frac{2}{5}w - 90e^{-t}$$

- (a) Show that

$$2\frac{d^2w}{dt^2} - 5\frac{dw}{dt} + 2w = 450e^{-t}$$

(3)

- (b) Find a general solution for the number of white-clawed crayfish at time  $t$  years. (6)
- (c) Find a general solution for the number of signal crayfish at time  $t$  years. (2)

The model predicts that, at time  $T$  years, the population of white-clawed crayfish will have died out.

Given that  $w = 65$  and  $s = 85$  when  $t = 0$

- (d) find the value of  $T$ , giving your answer to 3 decimal places. (6)
- (e) Suggest a limitation of the model. (1)







**Question 8 continued**

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**Question 8 continued**

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**(Total for Question 8 is 18 marks)**

**TOTAL FOR PAPER IS 75 MARKS**

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