

CANDIDATE
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MATHEMATICS

9709/03

Paper 3 Pure Mathematics 3 (P3)

For Examination from 2017

SPECIMEN PAPER

1 hour 45 minutes

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF9)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 75.

This document consists of **19** printed pages and **1** blank page.



4 The equation $x^3 - x^2 - 6 = 0$ has one real root, denoted by α .

(i) Find by calculation the pair of consecutive integers between which α lies. [2]

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(ii) Show that, if a sequence of values given by the iterative formula

$$x_{n+1} = \sqrt{\left(x_n + \frac{6}{x_n}\right)}$$

converges, then it converges to α . [2]

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(iii) Use this iterative formula to determine α correct to 3 decimal places. Give the result of each iteration to 5 decimal places. [3]

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(ii) Explain why the gradient of the curve is never negative. [1]

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(iii) Find the value of x for which the gradient is least. [1]

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7 The points A , B and C have position vectors, relative to the origin O , given by

$$\vec{OA} = \begin{pmatrix} 1 \\ 2 \\ 0 \end{pmatrix}, \quad \vec{OB} = \begin{pmatrix} 3 \\ 0 \\ 1 \end{pmatrix} \quad \text{and} \quad \vec{OC} = \begin{pmatrix} 1 \\ 1 \\ 4 \end{pmatrix}.$$

The plane m is perpendicular to AB and contains the point C .

- (i) Find a vector equation for the line passing through A and B . [2]

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- (ii) Obtain the equation of the plane m , giving your answer in the form $ax + by + cz = d$. [2]

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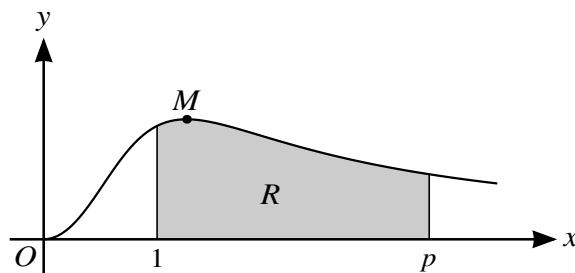
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The diagram shows the curve $y = \frac{x^2}{1+x^3}$ for $x \geq 0$, and its maximum point M . The shaded region R is enclosed by the curve, the x -axis and the lines $x = 1$ and $x = p$.

- (i) Find the exact value of the x -coordinate of M . [4]

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