## Probability Difficulty: Hard

## Question Paper 1

| Level | IGCSE |
| :--- | :--- |
| Subject | Maths (0580/0980) |
| Exam Board | CIE |
| Topic | Probability |
| Paper | Paper 4 |
| Difficulty | Hard |
| Booklet | Question Paper 1 |

Time allowed: 83 minutes
Score: /72
Percentage: /100

## Grade Boundaries:

CIE IGCSE Maths (0580)

| A* | A | B | C | D |
| :--- | :--- | :--- | :--- | :--- |
| $>83 \%$ | $67 \%$ | $51 \%$ | $41 \%$ | $31 \%$ |

CIE IGCSE Maths (0980)

| 9 | 8 | 7 | 6 | 5 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $>95 \%$ | $87 \%$ | $80 \%$ | $69 \%$ | $58 \%$ | $46 \%$ |

(a) A bag contains red beads and green beads.

There are 80 beads altogether.
The probability that a bead chosen at random is green is 0.35 .
(i) Find the number of red beads in the bag.
(ii) Marcos chooses a bead at random and replaces it in the bag. He does this 240 times.

Find the number of times he would expect to choose a green bead.
(b) A different bag contains 2 blue marbles, 3 yellow marbles and 4 white marbles.

Huma chooses a marble at random, notes the colour, then replaces it in the bag. She does this three times.

Find the probability that
(i) all three marbles are yellow,
(ii) all three marbles are different colours.
(c) Another bag contains 2 green counters and 3 pink counters.

Teresa chooses three counters at random without replacement.
Find the probability that she chooses more pink counters than green counters.


The diagram shows two fair dice.
The numbers on dice $A$ are $0,0,1,1,1,3$.
The numbers on dice $B$ are 1, 1, 2, 2, 2, 3.
When a dice is rolled, the score is the number on the top face.
(a) Dice $A$ is rolled once.

Find the probability that the score is not 3 .
(b) Dice $A$ is rolled twice.

Find the probability that the score is 0 both times.
(c) Dice $A$ is rolled 60 times.

Calculate an estimate of the number of times the score is 0 .
(d) Dice $A$ and dice $B$ are each rolled once.

The product of the scores is recorded.
(i) Complete the possibility diagram.

|  | 3 | 0 | 0 |  |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |
|  | 2 | 0 | 0 |  |  |  |
| Dice $B$ | 2 | 0 | 0 |  |  |  |

(ii) Find the probability that the product of the scores is
(a) 2,
(b) greater than 3 .
(e) Eva keeps rolling dice $B$ until 1 is scored.

Find the probability that this happens on the 5 th roll.

Each morning the probability that it rains is $\frac{2}{3}$.
If it rains, the probability that Asha walks to school is $\frac{1}{7}$.
If it does not rain, the probability that Asha walks to school is $\frac{4}{7}$.
(a) Complete the tree diagram.

(b) Find the probability that it rains and Asha walks to school.
(c) (i) Find the probability that Asha does not walk to school.
(ii) Find the expected number of days Asha does not walk to school in a term of 70 days.
(d) Find the probability that it rains on exactly one morning in a school week of 5 days.

Ravi spins a biased 5 -sided spinner, numbered 1 to 5 .
The probability of each number is shown in the table.

| Number | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Probability | $\frac{1}{6}$ | $\frac{1}{4}$ | $\frac{1}{3}$ | $x$ | $x$ |

(a) Find the value of $x$.
(b) Ravi spins the spinner once.

Find the probability that the number is 2 or 3 .
(c) Ravi spins the spinner twice.

Find the probability that
(i) the number is 2 both times,
(ii) the sum of the numbers is 3 .
(d) Ravi spins the spinner 72 times.

Calculate how many times he expects the number 1.

A train stops at station $A$ and then at station $B$.
If the train is late at station $A$, the probability that it is late at station $B$ is 0.9 .
If the train is not late at station $A$, the probability that it is late at station $B$ is 0.2 .
The probability that the train is late at station $A$ is 0.3 .
(a) Complete the tree diagram.

(b) (i) Find the probability that the train is late at one or both of the stations.
(ii) This train makes 250 journeys.

Find the number of journeys that the train is expected to be late at one or both of the stations.
(c) The train continues to station $C$.

The probability that it is late at all 3 stations is 0.27 .
Describe briefly what this probability shows.

The probability that a plant will produce flowers is $\frac{7}{8}$.
The flowers are either red or yellow.
If the plant produces flowers, the probability that the flowers are red is $\frac{3}{4}$.
(a) (i) Complete the tree diagram by writing a probability beside each branch.

(ii) Calculate the probability that a plant, chosen at random, will produce red flowers.
(iii) Two plants are chosen at random.

Calculate the probability that both will produce red flowers.
(b) Alphonse buys 200 of theseplants.

Calculate the number of plants that are expected to produce flowers.
(c) Gabriel has 1575 plants with red flowers.

Estimate the total number of plants that Gabriel has.

Sandra has a fair eight-sided spinner.
The numbers on the spinner are $3,4,4,4,5,5,6$ and 8 .
Sandra spins the spinner twice and records each number it lands on.


Find the probability that
(a) both numbers are 8 ,
(b) the two numbers are not both 8 ,
(c) one number is odd and one number is even,
(d) the total of the two numbers is at least 13 ,
(e) the second number is bigger than the first number.

