## Vectors

## Difficulty: Medium

## Question Paper 2

| Level | IGCSE |
| :--- | :--- |
| Subject | Maths (0580/0980) |
| Exam Board | CIE |
| Topic | Vectors |
| Paper | Paper 4 |
| Difficulty | Medium |
| Booklet | Question Paper 2 |

Time allowed: $\quad 109$ minutes
Score: /95

Percentage: /100

## Grade Boundaries:

CIE IGCSE Maths (0580)

| A* | A | B | C | D |
| :--- | :--- | :--- | :--- | :--- |
| $>83 \%$ | $67 \%$ | $51 \%$ | $41 \%$ | $31 \%$ |

CIE IGCSE Maths (0980)

| 9 | 8 | 7 | 6 | 5 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $>95 \%$ | $87 \%$ | $80 \%$ | $69 \%$ | $58 \%$ | $46 \%$ |


(a) Draw the image when triangle $A$ is reflected in the line $x=0$.
(b) Draw the image when triangle $A$ is rotated through $90^{\circ}$ anticlockwise about $(-4,0)$.
(c) (i) Describe fully the single transformation that maps triangle $A$ onto triangle $B$.
(ii) Complete the following statement.

Area of triangle $A$ : Area of triangle $B=$ $\qquad$ :...................
(d) Write down the matrix that represents a stretch, factor 4 with the $y$-axis invariant.
(e) (i) On the grid, draw the image of triangle $A$ after the transformation represented by the matrix $\left(\begin{array}{ll}1 & 0 \\ 2 & 1\end{array}\right)$.
(ii) Describe fully this single transformation.
(iii) Find the inverse of the matrix $\left(\begin{array}{ll}1 & 0 \\ 2 & 1\end{array}\right)$.

(a) Draw the reflection of shape $Q$ in the line $x=-1$.
(b) (i) Draw the enlargement of shape $Q$, centre $(0,0)$, scale factor -2 .
(ii) Find the $2 \times 2$ matrix that represents an enlargement, centre $(0,0)$, scale factor -2 .
(c) (i) Draw the stretch of shape $Q$, factor $2, x$-axis invariant.
(ii) Find the $2 \times 2$ matrix that represents a stretch, factor $2, x$-axis invariant.
(iii) Find the inverse of the matrix in part (c)(ii).
(iv) Describe fully the single transformation represented by the matrix in part(c)(iii).

(a) Describe fully the single transformation that maps shape $Q$ onto shape $R$.
(b) (i) Draw the image when shape $Q$ is translated by the vector $\binom{5}{4}$.
(ii) Draw the image when shape $Q$ is reflected in the line $x=2$.
(iii) Draw the image when shape $Q$ is stretched, factor 3, $x$-axis invariant.
(iv) Find the $2 \times 2$ matrix that represents a stretch of factor $3, x$-axis invariant.
(c) Describe fully the single transformation represented by the matrix $\left(\begin{array}{ll}0 & 1 \\ 1 & 0\end{array}\right)$.

(i) Describe fully the single transformation which maps shape $P$ onto shape $Q$.
(ii) On the grid above, draw the image of shape $P$ after reflection in the line $y=-1$.

On the grid above, draw the image of shape $P$ under the transformation represented by the
(iii)
matrix $\left(\begin{array}{cc}0 & -1 \\ 1 & 0\end{array}\right)$.
(b)

(i) Describe fully the single transformation which maps shape $M$ onto shape $L$.
(ii) On the grid above, draw the image of shape $M$ after enlargement by scale factor 2, centre $(5,0)$.

(a) (i) Draw the image of shape $A$ after a stretch, factor $3, x$-axis invariant.
(ii) Write down the matrix representing a stretch, factor $3, x$-axis invariant.
(b) (i) Describe fully the single transformation which maps shape $A$ onto shape $B$.
(ii) Write down the matrix representing the transformation which maps shape $A$ onto shape $B$.
(a) Calculate the magnitude of the vector $\binom{3}{-5}$.
(b)

(i) The points $P$ and $R$ are marked on the grid above.

$$
\overrightarrow{P Q}=\binom{3}{-5} . \text { Draw the vector } \overrightarrow{P Q} \text { on the grid above. }
$$

(ii) Draw the image of vector $\overrightarrow{P Q}$ after rotation by $90^{\circ}$ anticlockwise about $R$.
(c) $\overrightarrow{D E}=2 \mathbf{a}+\mathbf{b}$ and $\overrightarrow{D C}=3 \mathbf{b}-\mathbf{a}$.

Find $\overrightarrow{C E}$ in terms of $\mathbf{a}$ and $\mathbf{b}$. Write your answer in its simplest form.
(d) $\overrightarrow{O T}=\binom{-2}{5}$ and $\overrightarrow{O V}=\binom{5}{-1}$.

Write $\overrightarrow{T V}$ as a column vector.
(e)

$\overrightarrow{A B}=\mathrm{b}$ and $\overrightarrow{A C}=\mathbf{c}$.
(i) Find $\overrightarrow{C B}$ in terms of $\mathbf{b}$ and $\mathbf{c}$.
(ii) $X$ divides $C B$ in the ratio 1:3.
$M$ is the midpoint of $A B$.
Find $\overrightarrow{M X}$ in terms of $\mathbf{b}$ and $\mathbf{c}$.
Show all your working and write your answer in its simplest form.

## Question 7

(a)

(i) Draw the translation of triangle $X$ by the vector $\binom{-11}{-1}$.
(ii) Draw the enlargement of triangle $Y$ with centre $(-6,-4)$ and scale factor $\frac{1}{2}$
(b)


Describe fully the single transformation that maps
(i) triangle $X$ onto triangle $Z$,
(ii) triangle $X$ onto triangle $Y$,
(iii) triangle $X$ onto triangle $W$.
(c) Find the matrix that represents the transformation in part (b)(iii).

