# Trigonometry Difficulty: Medium 

## Question Paper 3

| Level | IGCSE |
| :--- | :--- |
| Subject | Maths (0580/0980) |
| Exam Board | CIE |
| Topic | Trigonometry |
| Paper | Paper 4 |
| Difficulty | Medium |
| Booklet | Question Paper 3 |

Time allowed: $\quad 91$ minutes

Score: /79
Percentage: /100

## Grade Boundaries:

CIE IGCSE Maths (0580)

| A* | A | B | C | D |
| :--- | :--- | :--- | :--- | :--- |
| $>83 \%$ | $67 \%$ | $51 \%$ | $41 \%$ | $31 \%$ |

CIE IGCSE Maths (0980)

| 9 | 8 | 7 | 6 | 5 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $>95 \%$ | $87 \%$ | $80 \%$ | $69 \%$ | $58 \%$ | $46 \%$ |


$A B C D$ is a quadrilateral and $B D$ is a diagonal.
$A B=26 \mathrm{~cm}, B D=24 \mathrm{~cm}$, angle $A B D=40^{\circ}$, angle $C B D=40^{\circ}$ and angle $C D B=30^{\circ}$.
(a) Calculate the area of triangle $A B D$.
(b) Calculate the length of $A D$.
(c) Calculate the length of $B C$.


The diagram shows some straight line distances between Auckland $(A)$, Hamilton $(H)$, Tauranga ( $T$ ) and Rotorua ( $R$ ).
$A T=180 \mathrm{~km}, A H=115 \mathrm{~km}$ and $H T=90 \mathrm{~km}$.
(a) Calculate angle HAT.

Show that this rounds to $25.0^{\circ}$, correct to 3 significant figures.
(b) The bearing of $H$ from $A$ is $150^{\circ}$.

Find the bearing of
(i) $T$ from $A$,
(ii) $A$ from $T$.
(c) Calculate how far $T$ is east of $A$.
(d) Angle $T H R=30^{\circ}$ and angle $H R T=70^{\circ}$.

Calculate the distance $T R$.
(e) On a map the distance representing $H T$ is 4.5 cm .

The scale of the map is $1: n$.
Calculate the value of $n$.


The diagram above shows the net of a pyramid.

The base $A B C D$ is a rectangle 8 cm by 6 cm .

All the sloping edges of the pyramid are of length 7 cm .
$M$ is the mid-point of $A B$ and $N$ is the mid-point of $B C$.
(a) Calculate the length of
(i) $Q M$,
(ii) $R N$.
(b) Calculate the surface area of thepyramid.
(c)


The net is made into a pyramid, with $P, Q, R$ and $S$ meeting at $P$.
The mid-point of $C D$ is $G$ and the mid-point of $D A$ is $H$.
The diagonals of the rectangle $A B C D$ meet at $X$.
(i) Show that the height, $P X$, of the pyramid is 4.90 cm , correct to 2 decimal places.
(ii) Calculate angle $P N X$.
(iii) Calculate angle $H P N$.
(iv) Calculate the angle between the edge $P A$ and the base $A B C D$.
(v) Write down the vertices of a triangle which is a plane of symmetry of the pyramid.


NOT TO
SCALE

The diagram shows a pyramid on a horizontal rectangular base $A B C D$. The diagonals of $A B C D$ meet at $E$.
$P$ is vertically above $E$.
$A B=8 \mathrm{~cm}, B C=6 \mathrm{~cm}$ and $P C=13 \mathrm{~cm}$.
(a) Calculate $P E$, the height of the pyramid.
(b) Calculate the volume of thepyramid.
[The volume of a pyramid is given by $\frac{1}{3} \times$ area of base $\times$ height.]
(c) Calculate angle $P C A$.
(d) $M$ is the mid-point of $A D$ and $N$ is the mid-point of $B C$.

Calculate angle MPN.
(e) (i) Calculate angle $P B C$.
(ii) $K$ lies on $P B$ so that $B K=4 \mathrm{~cm}$.

Calculate the length of $K C$.

NOT TO
SCALE


The diagram shows a pyramid on a rectangular base $A B C D$, with $A B=6 \mathrm{~cm}$ and $A D=5 \mathrm{~cm}$. The diagonals $A C$ and $B D$ intersect at $F$.
The vertical height $F P=3 \mathrm{~cm}$.
(a) How many planes of symmetry does the pyramid have?
(b) Calculate the volume of the pyramid.
[The volume of a pyramid is $\frac{1}{3} \times$ area of base $\times$ height.]
(c) The mid-point of $B C$ is $M$.

Calculate the angle between $P M$ and the base.
(d) Calculate the angle between $P B$ and the base.
(e) Calculate the length of $P B$.


Felipe $(F)$ stands 17 metres from a bridge $(B)$ and 32 metres from a tree $(T)$. The points $F, B$ and $T$ are on level ground and angle $B F T \# 40^{\circ}$.
(a) Calculate
(i) the distance $B T$,
(ii) the angle $B T F$.
(b) The bearing of $B$ from $F$ is $085^{\circ}$. Find the bearing of
(i) $T$ from $F$,
(ii) $F$ from $T$,
(iii) $B$ from $T$.
(c) The top of the tree is 30 metres vertically above $T$.

Calculate the angle of elevation of the top of the tree from $F$.

