## Probability formulae Question Paper 1

| Level | A LEVEL |
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| Exam Board | Edexcel |
| Subject | Mathematics |
| Module | Mechanics and Statistics |
| Topic | Conditional probability |
| Sub-Topic | Probability formulae |
| Booklet | Question Paper 1 |

Time Allowed:
43 minutes
Score: /38
Percentage:
/100

Grade Boundaries:

| A* | A | B | C | D | E | U |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $>85 \%$ | $77.5 \%$ | $70 \%$ | $62.5 \%$ | $57.5 \%$ | $45 \%$ | $<45 \%$ |

1 A contractor bids for two building projects. He estimates that the probability of winning the first project is 0.5 , the probability of winning the second is 0.3 and the probability of winning both projects is 0.2 .
(a) Find the probability that he does not win either project.
(b) Find the probability that he wins exactly one project.
(c) Given that he does not win the first project, find the probability that he wins the second.
(d) By calculation, determine whether or not winning the first contract and winning the second contract are independent events.

2 The events $A$ and $B$ are such that $\mathrm{P}(A)=\frac{2}{5}, \mathrm{P}(B)=\frac{1}{2}$ and $\mathrm{P}\left(A \mid B^{\prime}\right)=\frac{4}{5}$
(a) Find
(i) $\mathrm{P}\left(A \cap B^{\prime}\right)$,
(ii) $\mathrm{P}(A \cap B)$,
(iii) $\mathrm{P}(A \cup B)$,
(iv) $\mathrm{P}(A \mid B)$.
(b) State, with a reason, whether or not $A$ and $B$ are
(i) mutually exclusive,
(ii) independent.

3 A group of office workers were questioned for a health magazine and ${ }_{5}^{2}$ were found to take regular exercise. When questioned about their eating habits $\frac{2}{3}$ said they always eat breakfast and, of those who always eat breakfast $\frac{9}{25}$ also took regular exercise.

Find the probability that a randomly selected member of the group
(a) always eats breakfast and takes regular exercise,
(b) does not always eat breakfast and does not take regular exercise.
(c) Determine, giving your reason, whether or not always eating breakfast and taking regular exercise are statistically independent.

4 (a) State in words the relationship between two events $R$ and $S$ when $\mathrm{P}(R \cap S)=0$

The events $A$ and $B$ are independent with $\mathrm{P}(A)=\frac{1}{4}$ and $\mathrm{P}(A \cup B)=\frac{2}{3}$
Find
(b) $\mathrm{P}(B)$
(c) $\mathrm{P}\left(A^{\prime} \cap B\right)$
(d) $\mathrm{P}\left(B^{\prime} \mid A\right)$

