

Cambridge International Examinations

Cambridge International Advanced Subsidiary and Advanced Level

MATHEMATICS
Paper 2
May/June 2016
MARK SCHEME
Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol
 [↑] implies that the A or B mark indicated is allowed for work correctly following
 on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
 A and B marks are not given for fortuitously "correct" answers or results obtained from
 incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a "fortuitous" answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR −1 A penalty of MR −1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through \\^\mathrean" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR−2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

Р	age 4		Syllabus	Pap	
		Cambridge International AS/A Level – May/June 2016	9709	21	
		ain first derivative of form $k_1 e^{4x} + \frac{k_2}{2x+3}$		M1	
	Obta	ain correct $12e^{4x} - \frac{12}{2x+3}$		A1	
		ain 8		A1	[3
,		$\cot \theta = 1 \div \tan \theta$		B 1	
		in equation involving $\tan \theta$ only and with no denominators involving θ ain $\tan^2 \theta = \frac{2}{7}$		M1 A1	
		ain 28.1		A1	
	Obta	nin 151.9 ow other valid methods		A1	[5
3		rrange to $3e^{2x} - 14e^x + 8 = 0$ or equivalent involving substitution		B1	
		we quadratic equation in e^x to find two values of e^x ain $\frac{2}{3}$ and 4		*M1 A1	
		natural logarithms to solve equation of form $e^x = k$ where $k > 0$ dep on by M mark if left in exact form		DM1 M1	
	Obta	ain -0.405		A1	
	Obta	ain 1.39		A1	[6]
ļ	(i)	Carry out division, or equivalent, at least as far as $8x^2 + kx$		M1	
		Obtain correct quotient $8x^2 + 14x - 15$		A1	ΓΔ.
		Confirm remainder is 5		A1	[3]
	(ii)	State or imply expression is $(x+2)$ (their quadratic quotient)		B1 √	
		Attempt factorisation of their quadratic quotient		M1	

(i) Obtain $\frac{dx}{d\theta} = 2\sec^2\theta$ and $\frac{dy}{d\theta} = 6\cos 2\theta$ 5 **B**1 Use $\cos 2\theta = 2\cos^2 \theta - 1$ or equivalent **B**1 Form expression for $\frac{dy}{dx}$ in terms of $\cos \theta$ **M1** Confirm $6\cos^4\theta - 3\cos^2\theta$ with no errors seen

A1

B1√

A1

[3]

[1]

[4]

Obtain (x+2)(2x+5)(4x-3)

(iii) State $\pm \frac{3}{4}$ and no others, following their 3 linear factors

- (ii) Equate first derivative to zero and obtain at least $\cos \theta = \pm \frac{1}{\sqrt{2}}$ **B**1 Obtain $\theta = \frac{1}{4}\pi$ or equivalent **B**1 Obtain (2, 3) **B**1 [3]
- (iii) State or imply $\theta = \frac{1}{3}\pi$ or equivalent **B**1 Obtain $-\frac{3}{8}$ or equivalent only **B**1 [2]

F	age 5		Syllabus	Pap	er
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6	(i)	Use quotient rule or equivalent		*M1	
		Obtain $\frac{6x(x^2+4)-6x^3}{(x^2+4)^2}$ or equivalent		A1	
		Equate first derivative to $\frac{1}{2}$ and remove algebraic denominators dep on *M1		DM1	
		Obtain $48p = p^4 + 8p^2 + 16$ or $48x = x^4 + 8x^2 + 16$ or equivalent		A1	
		Confirm given result $p = \sqrt{\frac{48p - 16}{p^2 + 8}}$		A1	[5]
	(ii)	Consider sign of $p - \sqrt{\frac{48p - 16}{p^2 + 8}}$ at 2 and 3 or equivalent		M1	
		Complete argument correctly with appropriate calculations		A1	[2]
	(iii)	Carry out iteration process correctly at least once Obtain final answer 2.728		M1 A1	
		Show sufficient iterations to justify accuracy to 4 sf or show sign change in interval (2.7275, 2.7285)		B1	[3]
7	(a)	Rewrite integrand as $\sec^2 2x + \cos^2 2x$		B1	
		Express $\cos^2 2x$ in form $k_1 + k_2 \cos 4x$		M1	
		State correct $\frac{1}{2} + \frac{1}{2}\cos 4x$		A1	
		Integrate to obtain at least terms involving $\tan 2x$ and $\sin 4x$		M1 A1	[5]
		Obtain $\frac{1}{2} \tan 2x + \frac{1}{2}x + \frac{1}{8} \sin 4x$, condoning absence of $+c$		AI	[5]
	(b)	Integrate to obtain $2x + 2\ln(3x - 2)$		B 1	
		Show correct use of $p \ln k = \ln k^p$ law at least once, must be using $\ln(3x-2)$		M1	
		Show correct use of $\ln m - \ln n = \ln \frac{m}{n}$ law, must be using $\ln(3x - 2)$		M1	
		Use or imply $20 = \ln(e^{20})$		B 1	
		Obtain $ln(16e^{20})$		A1	[5]